

The Good

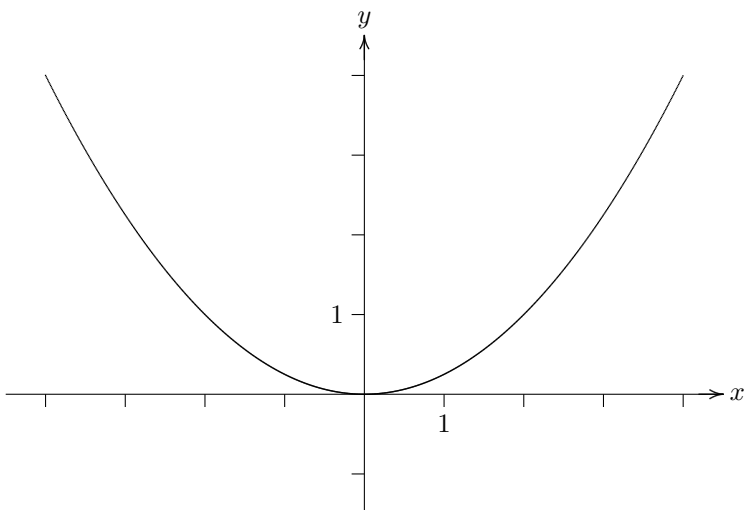
Perform the indicated operation and simplify: $\frac{2x+3}{x-\sqrt{2}} - \frac{x^2+1}{3}$.

$$\begin{aligned}\text{Now, } \frac{2x+3}{x-\sqrt{2}} - \frac{x^2+1}{3} &= \frac{3(2x+3)}{3(x-\sqrt{2})} - \frac{(x^2+1)(x-\sqrt{2})}{3(x-\sqrt{2})} \\ &= \frac{3(2x+3) - (x^2+1)(x-\sqrt{2})}{3(x-\sqrt{2})} \\ &= \frac{6x+9 - (x^3 - (\sqrt{2})x^2 + x - \sqrt{2})}{3(x-\sqrt{2})} \\ &= \frac{6x+9 - x^3 + (\sqrt{2})x^2 - x + \sqrt{2}}{3(x-\sqrt{2})} \\ &= \frac{-x^3 + (\sqrt{2})x^2 + 5x + (9 + \sqrt{2})}{3(x-\sqrt{2})}.\end{aligned}$$

Comments:

- Note that the equal signs *neatly* lined up and on the same level as the fraction bars of the fractions.
 - Note that each step is a single simplification. Multiple simplifications carried out in the same step can easily lead to confusion and, worse, errors.
 - Note how the terms in the numerator have been collected in descending degree.
 - Note the parentheses around the “ $\sqrt{2}$ ” to emphasize that it is the coefficient of x^2 and to make sure that the x^2 is not accidentally placed under the radical along with the 2.
 - Note that the denominator has been left in *factored form* and, furthermore, GASP!!, a radical has been left in the denominator.
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Graph $y = \frac{1}{4}x^2$.



Comments:

- Note that the axes are labeled and arrows appear **ONLY** in the positive direction.
- Note that the tick marks are *evenly* spaced and that the scales on the two axes *agree*.
- Note that the tick marks have been *minimally* labeled.
- Note that the ends of the graph do **NOT** have arrows – the graph is *assumed* to continue indefinitely.
- Note that the graph is not tiny.
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